## Electronic structure and ferromagnetism of Mn-substituted CuAlS<sub>2</sub>, CuGaS<sub>2</sub>, CuInS<sub>2</sub>, CuGaSe<sub>2</sub>, and CuGaTe<sub>2</sub>

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The electronic and magnetic properties of Mn doping at either cation sites in the class of I–III–VI $_2$  chalcopyrites are studied by first-principles calculation. It is found that Mn doping at the III site provides holes and stabilizes the ferromagnetic interaction between neutral Mn defects; the neutral Mn $_{Cu}^0$  also stabilizes the ferromagnetism, although it provides electrons to the conduction band, instead of holes. The ferromagnetic stability is generally weaker when the cation or the anion becomes heavier in these chalcopyrites, i.e., along the sequences  $CuAlS_2 \rightarrow CuGaS_2 \rightarrow CuInS_2$  and  $CuGaS_2 \rightarrow CuGaSe_2 \rightarrow CuGaTe_2$ . Interestingly,  $CuAlO_2$  in the chalcopyrite structure is predicted to have lower FM energy than  $CuAlS_2$  despite its lighter anion and shorter bonds. In general, III site substitution gives stabler ferromagnetism than Cu substitution. Thus, the preferred growth conditions are Cu-rich and III-poor, which maximize  $Mn_{III}$  replacement. In n-type samples, when  $Mn_{III}$  is negatively charged, the antiferromagnetic coupling is preferred. In p-type samples, the ground state of positively charged  $Mn_{Cu}^+$  is also antiferromagnetism. The main feature of the calculated electronic properties of Mn defect at either Cu or III site is explained using a simple picture of dangling bond hybride and crystal-field resonance.

DOI: 10.1103/PhysRevB.69.104422 PACS number(s): 75.50.Pp, 75.30.Hx, 75.10.Dg

## I. INTRODUCTION

Ferromagnetism in Mn-substituted semiconductors is thought to arise from the interaction of a hole with the local moment of the *d* electrons of Mn. <sup>1,2</sup> In II–VI's such as CdTe or ZnSe, the substitution of Mn<sup>2+</sup> on the *divalent* cation site introduces no holes, so ferromagnetism (FM) is not observed. <sup>3</sup> If the system is additionally doped by extrinsic *p*-type dopant (e.g, As-on-VI site), weak FM is observed. <sup>4</sup> In III–V's such as GaAs, the substitution of Mn<sup>2+</sup> on the *trivalent* cation site does automatically introduce a hole, so FM is observed, even without additional *p*-type doping. In the ternary pnictide system A<sup>II</sup>M<sup>IV</sup>X<sub>2</sub><sup>V</sup> such as CdGeP<sub>2</sub> or the ternary pnictide system A<sup>II</sup>M<sup>IV</sup>X<sub>2</sub><sup>V</sup> such as CdGeP<sub>2</sub> or the ternary pnictide system A<sup>II</sup>M<sup>IV</sup>X<sub>2</sub><sup>V</sup> such as CdGeP<sub>2</sub> or the ternary pnictide system A<sup>II</sup>M<sup>IV</sup>X<sub>2</sub><sup>V</sup> such as CdGeP<sub>2</sub> or the ternary pnictide system A<sup>II</sup>M<sup>IV</sup>X<sub>2</sub><sup>V</sup> such as CdGeP<sub>2</sub> or the ternary pnictide system A<sup>II</sup>M<sup>IV</sup>X<sub>2</sub><sup>V</sup> such as CdGeP<sub>2</sub> or the ternary pnictide system A<sup>II</sup>M<sup>IV</sup>X<sub>2</sub><sup>V</sup> such as CdGeP<sub>2</sub> or the ternary pnictide system A<sup>II</sup>M<sup>IV</sup>X<sub>2</sub><sup>V</sup> such as CdGeP<sub>3</sub> or the ternary pnictide system A<sup>II</sup>M<sup>IV</sup>X<sub>2</sub><sup>V</sup> such as CdGeP<sub>3</sub> or the ternary pnictide system A<sup>II</sup>M<sup>IV</sup>X<sub>2</sub><sup>V</sup> such as CdGeP<sub>3</sub> or the ternary pnictide system A<sup>II</sup>M<sup>IV</sup>X<sub>3</sub><sup>V</sup> such as CdGeP<sub>3</sub> or the ternary pnictide system A<sup>II</sup>M<sup>IV</sup>X<sub>3</sub><sup>V</sup> such as CdGeP<sub>3</sub> or the ternary pnictide system A<sup>II</sup>M<sup>IV</sup>X<sub>3</sub><sup>V</sup> such as CdGeP<sub>3</sub> or the ternary pnictide system A<sup>II</sup>M<sup>IV</sup>X<sub>3</sub><sup>V</sup> such as CdGeP<sub>3</sub> or the ternary pnictide system A<sup>II</sup>M<sup>IV</sup>X<sub>3</sub><sup>V</sup> such as CdGeP<sub>3</sub> or the ternary pnictide system A<sup>II</sup>M<sup>IV</sup>X<sub>3</sub><sup>V</sup> such as CdGeP<sub>3</sub> or the ternary pnictide system A<sup>II</sup>M<sup>IV</sup>X<sub>3</sub><sup>V</sup> such as CdGeP<sub>3</sub> or the ternary pnictide system A<sup>II</sup>M<sup>IV</sup>X<sub>3</sub><sup>V</sup> such as CdGeP<sub>3</sub> or the ternary pnictide system as CdGeP<sub>3</sub>

nary chalcopyrite system  $A^{I}M^{III}X_2^{VI}$  such as CuAg-10.1 6.985 0 0 6.985 247.55 0 285131 .420Tc [(sv9996 T-1.2165 T-1.23 Tmthe)-3IVMi

the  $t_2$  levels split into  $t_a = d_{xz}$ ;  $d_{yz}$  and  $t_b = d_{xy}$ . We find that the electron actually resides in a level that mixes  $e_b$  with  $t_b$  character, rendering to it some delocalized  $t_2$ -like character. Thus, Mn on Cu site also introduces ferromagnetism. The ferromagnetic stability for Mn on the Cu site is generally lower than for Mn on the III site, with minor exceptions. The order of ferromagnetic stability for Mn-on-Cu (for Mn atoms being fourth neighbors) is reduced in the series CuGaSe<sub>2</sub>  $\rightarrow$  CuGaSe<sub>2</sub>  $\rightarrow$  CuGaTe<sub>2</sub>  $\rightarrow$  CuAlS<sub>2</sub>  $\rightarrow$  CuInS<sub>2</sub>.

(iii) Ferromagnetism depends on the orientation of the Mn atoms within the chalcopyrite lattice. The highest stabilization exists for Mn atoms oriented along the  $\langle 110 \rangle$  direction,

e.g., one Mn at (2or Mn atoms86.6(10.457T032rsrec5-167dec.96xi 0 Tf rsrecws24o26n3271duces)271-i4 /F2ei95.439-8ngat

pure host chalcopyrites. We calculated the ideal bond length, Al–S (2.27 Å), Ga–S (2.30 Å), Ga–Se (2.43 Å), Ga–Te (2.63 Å), and In–S (2.50 Å), in very good agreement (less than 2% difference) with the measured bond length listed in Ref. 20. Substitution of Mn on the column III site creates a *shorter* bond with S in CuAlS<sub>2</sub>, a *longer* bond in CuInS<sub>2</sub>, but in CuGaS<sub>2</sub>, CuGaSe<sub>2</sub>, or CuGaTe<sub>2</sub>, the bonds are unchanged by Mn substitution, suggesting a similar tetrahedral radius for Ga and Mn in those compounds.

Figure 1(a) shows the Mn 3d projected local density of states (LDOS). Going from deeper to shallower levels, we see the sequence  $e_+^{\text{CFR}} \!\!\to\! t_+^{\text{CFR}} \!\!\to\! t_-^{\text{DBH}} \!\!\to\! t_+^{\text{DBH}} \!\!\to\! e_-^{\text{CFR}} \!\!\to\! e_+^{\text{CFR}}$ . The labeling "dangling bond hybride" (DBH) and "crystalfield resonance" (CFR) will be explained in the following and Figs. 2(a) and 2(b) show, respectively, the spin-up and spin-down wave function square at  $\Gamma$  of these states. We see the following:

(i) The  $e^{\text{CFR}}$  states are e-like, i.e., have lobes that point in-between the nearest neighbors. Those state are highly lo-

calized on Mn, and can be thought of as nonbonding. The lowest state  $e_+^{\rm CFR}$  lies deep inside the host valence band and

The overall electron configurations of  $\mathrm{Mn_{Al}^0}$  can thus be designated as  $[e_+^2t_+^3]_{\mathrm{CFR}}(t_-^3t_+^2)_{\mathrm{DBH}}[e_-^0t_-^0]_{\mathrm{CFR}}$ . The total moment is thus  $\mu = 2 + 3 - 3 + 2 = 4$ . Since the CFR states are Mn-localized and carry five spin-up electrons, whereas the DBH is more extended, and carries a hole, such a ground state is often designated as " $d^5+$  hole." It is interesting to compare the degree of localization of up-spin vs down spin states. Figure 2 shows that  $t_-^{\mathrm{DBH}}$  is more delocalized than  $t_+^{\mathrm{DBH}}$ .

Since  $\operatorname{Mn_{Al}^0}$  contains a hole at the  $t_+^{\operatorname{DBH}}$  state, raising the Fermi energy  $E_F$  via n-type doping will lead to the capture of an electron from the Fermi sea into this orbital, transforming  $\operatorname{Mn_{Al}^0}$  to  $\operatorname{Mn_{Al}^-}$ . The change in total energy for this acceptor reaction is the acceptor transition energy E(0/-), and is calculated as explained in Sec. II and Eq. (2). Figure 3(a) shows the calculated acceptor level for  $\operatorname{Mn_{III}}$  in a few chalcopyrites. We see that all the acceptor levels of  $\operatorname{Mn_{III}}$  are ranging between 180 and 350 meV. The acceptor level becomes progressively shallower along the series  $\operatorname{CuGaS_2} \to \operatorname{CuAlS_2} \to \operatorname{CuGaSe_2} \to \operatorname{CuGaTe_2} \to \operatorname{CuInS_2}$ .

The electronic structure of Mn<sub>Al</sub> obtained through numerical calculations [Figs. 1(a) and 2 can be explained qualita-

Å), and Cu-Te (2.55 Å)

(iii) In the case of  $Mn_{Cu}$  we have the DBH electrons deep in the valence band below  $t_+^{CFR}$ , whereas in  $Mn_{Al}$  they were near the VBM, above  $t_+^{CFR}$ . The  $t_-^{DBH}$  states, shown around  $E_{VBM}$  – 1.8 eV, are occupied by three spin-up and three spindown electrons. Inspection of the LDOS in the S next to Mn show that those DBH states have small spin splitting, are mostly anion-like, and are mostly contributed from off- $\Gamma$ point wave functions (and thus are not seen in the  $\Gamma$  point wave function plot of Fig. 5). The order of levels for  $Mn_{Cu}^0$ going from deep to shallower levels is thus,  $t_{+}^{\text{DBH}} \rightarrow t_{-}^{\text{DBH}}$  $\rightarrow e_{+}^{CFR} \rightarrow t_{+}^{CFR} \rightarrow e_{-}^{CFR}$ , quite different from the order in  $\mathrm{Mn}_{\mathrm{Al}}^{0}$ . The formal configuration  $(t_{+}^{3}t_{-}^{3})_{DBH}[e_{+}^{2}t_{+}^{3}e_{-}^{1}]_{CFR}$  with a moment of 3-3+2+3-1=4  $\mu_{\rm B}$  and an electron in  $e_{-}$ . However, because the tetragonal crystal-field splitting of the e and  $t_2$  levels is large in Mn<sub>Cu</sub>, there is a secondary coupling between the split components  $e_b(d_{x^2-y^2})$  and  $t_b(d_{xy})$ , which is allowed by the reduced symmetry due to the Mn defect. Thus,

the electron resides in a level that is  $(\frac{2}{3}d_{x^2-y^2})$  and  $(\frac{1}{3}d_{xy})$ . Consequently, the electron at  $E_F$  does have some  $t_2$ -like character. Figure 3 shows that the donor level of Mn<sub>Cu</sub> is very deep (more than 710 meV) for all these chalcopyrites.

The electronic structure of Mn<sub>Cu</sub> obtained through numerical calculations can be explained qualitatively by a simple model [Fig. 4(b)]. Here, we first note that whereas the dangling bond  $t_2$  orbital of the Al vacancy in CuAlS<sub>2</sub> lies above the VBM, that due to a Cu vacancy lies about 1.90 eV below the host VBM.<sup>21</sup> Thus, in Fig 4(b), we placed the t(p)level below the t(d) level of Mn. This order of unperturbed levels produces the level scheme seen in our calculation. The  $t_{+}(p)$  level of the host hybridize with the  $t_{+}(d)$  level of the impurity to give the deep  $t_{+}^{DBH}$  bonding level, and the  $t_{+}^{CFR}$ antibonding level. Note that for Mn<sub>Al</sub> the order is reverted, since  $t_{+}(d)$  is below  $t_{+}(p)$ . Similarly, the  $t_{-}(p)$  level of the host hybridize with the  $t_{-}(d)$  level of the impurity to yield the bonding  $t_{-}^{\mathrm{DBH}}$  and antibonding  $t_{-}^{\mathrm{CFR}}$ . Like in  $\mathrm{Mn_{Al}}$ , here too the  $e_{-}^{\mathrm{CFR}}$  and  $e_{+}^{\mathrm{CFR}}$  levels are mostly unperturbed. Thus, the fact that the host dangling bond  $V_{\rm Cu}$ is deeper than the host dangling bond  $V_{\rm Al}$  leads to the different level ordering for Mn-on-Al [Fig. 4(a)] and Mn-on-Cu [Fig. 4(b)].

## IV. FERROMAGNETIC AND ANTIFERROMAGNETIC ENERGIES FOR TWO Mn IN CHALCOPYRITES

So far we have considered a single Mn atom per supercell, for studying the electronic structure. To study the magnetic ground state, we have placed two Mn atoms in a 64 atom chalcopyrite supercell, and computed the total energies for the ferromagnetic  $E_{\rm FM}$  and antiferromagnetic  $E_{\rm AFM}$  spin arrangement. We studied several possible configurations for a Mn pair in these chalcopyrites. The calculated  $\Delta E_{\rm FM}$  $=E_{\rm FM}-E_{\rm AFM}$  of different Mn pair configurations for CuAlS<sub>2</sub>, CuGaS<sub>2</sub>, CuInS<sub>2</sub>, CuGaSe<sub>2</sub>, and CuGaTe<sub>2</sub> are listed in Table II. The total energy of the most stable configuration for Mn doped at III site or at the Cu site is taken in Table II as reference energy. The pseudopotential results using ultrasoft potentials are in excellent agreement with the previous all-electron full-potential linearized augmented plane wave (FLAPW) calculations.<sup>22,8</sup> The latter calculation gives  $\Delta E_{\rm FM}$  of -77 and -64 meV for Ga440 in CuGaS<sub>2</sub> and CuGaSe<sub>2</sub>, respectively, whereas current pseudopotential calculation gives -81 and -61 meV, respectively. This indicates that the pseudopotential calculation is appropriate to give a reasonable description of the magnetic properties of Mn doped chalcopyrites. Table II shows the following:

(i) Chemical trends of FM: The ferromagnetic state is favored ( $\Delta E_{\rm FM}$ <0) for all the *neutral* charge states when Mn substitutes either the Cu or the column III site.<sup>23</sup> In general, III-substitution gives stabler FM than Cu-substitution. Thus, the preferred growth conditions for FM are Cu-rich and III-poor. The sample should not be strongly *n*-type (i.e., avoid excessive S deficiency) because then the acceptor will

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distance: the Mn–Mn distance for Cu022 is reduced to 2.83 Å from their ideal distance (3.77 Å), and one bonded S atom is pushed away from each Mn by more than 0.40 Å. In contrast, for the AFM phase of Cu022 in CuAlS<sub>2</sub>, the Mn–Mn distance is 3.57 Å, not far from its ideal value.

(v) Charge dependence of FM: When the charge state of  $\operatorname{Mn}_{\operatorname{Al}}^q$  changes from q=0 (holes in the DBH) to q=-1 (no holes), the FM disappears, and the ground state is AFM. The same is true for  $\operatorname{Mn}_{\operatorname{Cu}}^q$  when a changes from q=0 (electron carriers in conduction band) to q=+1 (no electron carriers). This means that when the material is doped excessively n-type, the hole will disappear and FM will vanish. In chal-