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# Anomalous Behavior of the Nitride Alloys

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provide structural coordinates, in that a  $\mathsf{R}^\mathsf{AB}_\mathsf{S}$  versus  $\mathsf{R}^\mathsf{AB}_\mathsf{p}$  amap° distinguishes predictively all different crystal structures of the binary AB compounds with 96% accuracy! Recently, Villars and Calvert [3] have extended this dual coordinate map into a threecoordinate map, thus separating thousands of compounds.

A recent development in this area is of interest to nitrides: Yeh et al. [4], calculated very precisely, using first-principles LDA, the difference in total energy between the ZB and WZ crystal structure of C, Si, GaAs, GaP, AlAs, AlP, GaN, AlN, InN, ZnS, ZnSe, and CdS. Remarkably, they found that the energy difference  $E_{\rm WZ}^{\rm AB}$   $\rm \ddot{\rm y}\,E_{ZB}^{\rm AB}$  has a linear scaling with the atomic orbital radii! Thus, it is now possible not only to predict which AB compound forms in ZB and which forms in WZ [1, 2], but one can also predict, just by knowing the atomic orbital radii of atom A and atom B (tabulated, e.g., in Ref. [2]), what is the  $WZ_{\pm}ZB$  energy difference for any AB compound (even hypothetical materials). This study revealed the tendency to stabilize the ZB structure in the series  $B<sup>V1</sup> \cap O$ ! S! Se! Te in  $A<sup>H1</sup>B<sup>V1</sup>$  and in  $A<sup>H1</sup> \cap G$  a! Al! In for  $A<sup>H1</sup>B<sup>V</sup>s$ , and proposed new, low temperature structures for CdSe(ZB) and MgTe(NiAs, not WZ).

> 3. Indirect ! Direct Band Gap Reversal in ZB ! WZ Structures of AlN, GaP

While the difference in total energies between the ZB and WZ crystal structures is only 10 meV/atom (consistent with the fact that the two structures are identical for the first two neighbor shells), the difference in band gap energy between the ZB and WZ crystal structures can be (e.g., SiC) as large as 1000 meV. This surprising effect was explained by Yeh et al. [5], in terms of direct±indirect band folding. They predicted that while AIN and GaP both have an indirect gap in the ZB structure, in the WZ structure the band gap will become direct. Can GaP be stabilized in the WZ structure? If so, it will have a direct band gap.

## 4. <sup>a</sup>Normal<sup>o</sup> versus <sup>a</sup>Anomalous<sup>o</sup> Isovalent Alloys

Before we show how <sup>a</sup>anomalous<sup>o</sup> the nitride alloys are, let us define what is a <sup>a</sup>normal<sup>o</sup> alloy. In a <sup>a</sup>normal<sup>o</sup> isovalent  $A_xB_{1yx}$  alloy, as one increases the composition x from zero, the conduction band moves as a whole, the valence band moves as a whole, and no new (defect) levels appear in the band gap. Furthermore, the bowing coefficient b in

# $E<sub>q</sub>...xt$   $\hat{ }$  x $E<sub>A</sub>$   $\uparrow$  ...1  $\ddot{y}$  xt  $E<sub>B</sub>$   $\ddot{y}$  bx...1  $\ddot{y}$  xt

is  $a<sup>3</sup>$ small<sup>o</sup> (less than 1 eV), and composition-independent. Also, normal isovalent alloys retain, to a large degree, the translational invariance of the underlying compounds A and B, even though the alloy is random. This behavior can be quantified by  $a$  projectingº a calculated random alloy wave function onto the Bloch orbitals of the constituent [6]. If a single wave vector k (ªmajority representationº) dominates the projection, then we can say that the alloy wave function retains the  $a$ -personality<sup>o</sup> of the parent components. The existence of a single dominant wave vector k in each alloy wave function means that the alloy states are extended and translationally nearly invariant.

ªNormalº isovalent alloys are usually made of components whose properties are <sup>a</sup>similar<sup>o</sup>, e.g., the band offsets are below 1 eV and the lattice mismatch is below say, 5%. In contrast, the valence band offset between  $GaAs<sub>±</sub>GaN$  is 2.3 eV, and the lattice constant mismatch is

lower than that of GaAs, addition of GaN creates nitrogen states only deep in the GaAs valence band. Indeed, our first principles calculations [11, 12] show a dramatic localization of the wave function of the CBM near the nitrogen atoms. This localization causes a giant (  $20 \text{ eV}$ ) bowing coefficient b...xt which also depends on composition x [12]. Our analysis of the wave functions of GaAs: N show that there are a few new states [13].

#### 6.1 The conventional  $a_1(N)$  state

In the impurity limit ... x ! 0), nitrogen induces a resonant impurity state  $a_1(N)$  inside the conduction band of GaAs. We find that this state exhibits nitrogen localization: nearly half of the charge of the  $a_1(N)$  state is contained inside the nearest-neighbor shell surrounding the nitrogen atom. This localization in real space is reflected in delocalization in reciprocal space, evidence by the spectral projection (only 15% of the wave function is due to G). In this impurity limit we find this state to be 180 meV above the CBM, in good agreement with the experimental estimate 150 to 180 meV. However, the energy of this  $a_1(N)$  state rises rapidly as the nitrogen composition increases. Thus, in the alloy ... x & 1%)  $a_1(N)$  is too far in energy to be important optically.

## 6.2 The perturbed host states

Substitution of N on As site exerts such a large perturbation that the host crystal states  $G_{1c}$ ,  $L_{1c}$  and  $X_{1c}$  mix thoroughly, forming new low-energy states. From the point of view of symmetry, substitution at a  $T_d$  symmetry site modifies the  $G_{1c}$  state  $a_1...G_{1c}$ , splits the fourfold  $L_{1c}$  valley

 $a_1(L_{1c})$ 

3. InGaN does not exhibit vanishing solubility, as expected from bulk-thermodynamic models. The surface-induced solubility is rather high.

4. InGaN exhibits localizatiaon of the hole wave functions. This could explain exciton localization even without atomic clustering. This leads to large (1 to 5 eV) and composition-dependent bowing coefficient.

5. Ga $\underline{As}$ : N exhibits localization of its electron wave function, giant (up to 20 eV) bowing coefficients, flattening of the band-gap pressure coefficient, increase of the electron effective-mass with pressure. This is explained by a G±X±L mixing and level anticrossing.

6. Atomic short-range order changes the band gap of GaAsN and GaInN much more strongly than in conventional GaAsP and GaInAs alloys. This is explained by wave function localization.

7. As the alloy composition in  $GaAs_{1yx}N_x$  reaches the (unfortunately impractical) percolation value of x 19%, we predict a transition in bond lengths and bulk modules, resulting from the formation of an uninterupted, wall-to-wall chain of  $Ga \pm N$ bonds.

8. P and As form deep isovalent gap levels in GaN.

9. P±P pairs and As±As pairs fill the band gap of GaN by a large number of levels forming a spectroscopic series. G-2.446 D(As)o4owledg0u5p4j1.436 0 gTD(serihe)Tj1.755 0 TD(ba