# Theoretical predictions of electronic materials and their properties

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In this article, I first define the basic structure of modern 'firstprinciples theory of real materials' (including old references), and then I review recent applications to electronic materials. I argue that electronic structure theory of real materiale has advanced to the point where bold predictions of yet unmade materials and of unsuspected physical properties are being made, fostering a new type of interaction with experimentalists. I review the basic characteristics of this new style of theory, illustrating a few recent applications, and express opinions as to future challenges.

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#### Abbreviations

СВМ	conduction band minimum
EMA	effective mass approximation
LAPW	linear augmented plane wave
LDA	local density approximation
LMTO	linear muffin tin orbital
VBM	valence band minimum
ΔH <sup>f</sup>	formation enthalpy
∆H <sup>m</sup>	migration enthalpy
ΔΕν	valence band offset

# Introduction The scope and structure of first-principles theory of 'real materials'

aims at understanding material properties and processes from an atomistic quantum-mechanical point of view, retaining the complexity and specificity of actual solids, without loosing track of the underlying global trends and basic physics.

## What's done?

The basic structure of electronic structure theory is drawn from text-book quantum-mechanics. A 'system' (atom, molecule, solid, nanostructure) is defined via its 'external means  $\frac{1}{2} \frac{V}{V}$  (c) which includes information on the structure

(e.g. electric, magnetic) fields. One then sets up an effective single-particle Schroedinger equation:

where  $V_{screening}$  is the systems response to  $V_{ext}$ . The screening potential, depends on the density matrix  $\rho$ . Where  $\{\Psi_i\}, \{\varepsilon_i\}$  are the single-particle wavefunctions and energies, respectively. Assuming at first a given geometry (hence, a given  $V_{ext}$  (r)) and using a specific microscopic model of screening (e.g. the local density approximation [LDA] [1]), one solves Equation 1 iteratively, using the boundary conditions appropriate to the system at hand (e.g. periodic bulk solids, isolated quantum dots, etc.). Iterations are needed because  $V_{screening}$  depends on  $\rho$  and the latter is obtained from the wavefunctions  $\Psi$  via  $\rho(\mathbf{r}, \mathbf{r}') = \sum_{i} \Psi_i^*(\mathbf{r})\Psi_i(\mathbf{r}')$ . The sequence is; one assumes  $\rho$ , then computes  $V_{screening}(\rho)$ , then solves Equation 1 to find  $\{\Psi_i\}$ , then recomputes a new  $\rho$  from the latter, and continues to public matrix  $\Phi$ .

obtains the total electron + nuclear energy [2] of that geometry:

$$\mathbf{E}_{ioi}\left\{R_{\alpha}, \alpha = 1...\mathbf{N}\right\} = \sum_{i} \epsilon_{i} - \frac{1}{2}\mathbf{E}_{H} - \frac{1}{4}\mathbf{E}_{XC} + \frac{1}{2}\mathbf{E}_{i-i} \qquad (2)$$

where the first term is the sum of single particle energies,  $E_H$  is the electron-electron Coulomb (Hartice) energy,  $E_{XC}$  is the exchange-correlation energy, and  $E_{i-i}$  is the ion-ion-energy. The forees on all N atoms are then obtained from  $E_{tot}$ ; one seeks the geometry that produces no forces:

$$\mathbf{F}_{\alpha} = \partial \mathbf{E}_{tot} / \partial R_{\alpha} = 0 \tag{3}$$

#### What's the input and what's the output?

Given the inputs, the N atomic number  $\{Z_{\alpha}\}$  and initial

the 'system' equilibrium geometry  $\{R_{\alpha}\}$ , its eigenvalue spectrum  $\{\epsilon_i\}$ , and total energy. Second derivatives of the total energy with respect to unit cell deformations yield elastic constants  $\{C_{ij}\}$ , whereas second derivatives with respect to collective atomic displacements yield force constants, hence the phonon spectrum. Bonding information is gleaned from the charge-density.

$$\rho(\mathbf{r}) = \sum_{i} \psi_{i}^{*}(\mathbf{r}) \psi_{i}(\mathbf{r})$$

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methods [3]. This yields quantities such as pressure equation of states, strain deformation potentials, and polarizabilities. When the eigenvalues  $\{\varepsilon_i\}$  are interpreted

 $-\frac{1}{2}\mathbf{V}^{2} + \mathbf{V}_{ext}(\mathbf{r}) + \mathbf{V}_{screening}(\mathbf{r}, \boldsymbol{\rho}) \{ \Psi_{i}(\mathbf{r}) = \boldsymbol{\varepsilon}_{i} \Psi_{i}(\mathbf{r}) \}$ (1)

the systems energy level structure, the transition matrix

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## What want it reacible?

structure of matter.

as from progress in computer technology. The main enabling steps are as follows:

1. The formulation of  $V_{screening}$  in terms of the density  $\rho$  by Kohn and Sham [1].

2. The evaluation of the functional form of useful approximation to  $V_{screening}$  { $\rho$ }, for example, the early exchange and correlation functional of Singwi *et al.* [4] and of Hedin and Lundqvist [5], and the most accurate one by Ceperley and Alder [6], and Perdew and Zunger [7].

3. The simplification of  $V_{ext}$  in terms of atomic pseudopotentials [8] that are calculable from well-defined (e.g. LDA) atomic models, [9–11] rather than empirically [12].

4. The formulation of nondivergent methods for evaluating  $E_{tot}$  and  $F_{\alpha}$  of infinite systems (e.g. in momentumspace) [2].

5. The development of efficient computational strategies to solve Equation 1, once general forms of  $V_{ext}$  and  $V_{screening}$  are formulated. This includes plane-wave methods (e.g. [2]), LAPW (linear augmented plane wave) [13] and LMTO (linear muffin tin orbital) [14,15].

matrix problems underlying Equation 1, for example, iterative-diagonalization, [16,17] and conjugate gradient [18].

7. The development of strategies for displacing atoms (Equation 3) simultaneously with refining charge densities

the latter [19] with molecular dynamics by Car and Parrinello [20].

parallel architectures.

# The characteristics of current first-principles

the classic solid state text books in a number of important ways.

ting the right answer for the wrong reason,' because there are now a number of independent approaches that systematically give the same answers. These are the LAPW and converged pseudopotential calculations (unfortunately, there are still quite a few LDA-based methods around that are poorly implemented producing unreliable results.)

#### **Realism is key**

Text-book simplifications including one-dimensional models; spherical-potentials; nearly free-electron models; simple tight-binding and other 'elegant' and 'back of the envelope' constructs have given way to an approach that tackles the real complexity and diversity of matter, without loosing sight of the underlying physics.

#### The approach is reflective

Discrepancies with experiments are analyzed by searching for specific inappropriate physical inputs/assumptions, rather than by using empirical adjustments to cover-up our basic incorrance For example when a 'user' terd are was calculated carly on [21] for LIF (9.0 eV, instead of the measured and previously calculated 14.2 eV) using a 'right' method (LDA with no adjustments [21]), the analysis of this shocking discrepancy led to a deeper understanding of fundamental (self-interaction) corrections [21] to the undertwing formalism. Similar discrepancies led laterem-

band structure.

#### The attitude is bold and interactive

This type of theory sometimes predicts unsuspected stable structures, or materials with previously unknown prop-

between the theoretical prediction and its experimental testing is often shorter than the duration of a PhD thesis.

described above characterize mostly the electronic structure theory of 'electronic materials,' that is semiconductors. Indeed, the structure-function relationships underlying

# Theory predicts defect properties in III-V nitrides

and dynamic conclations play a more crucial for

gral evaluation approximations), but focuses instead on

Nieminen [27] have used the pseudopotential LDA

	approach to study the properties of defects in GaN. The	low formation enthalpy H <sup>+</sup> center. High temperature and
	(via acceptors) and n-type doping (via donors). The theory gives access to five basic quantities: firstly, the lowest-energy location and geometries of the defect in the detection of the second sec	donor-acceptor pair, and recover the p-type benavior. <b>Opinion</b> Those valuations are executed at a high lavel of compar-
	lower $\Delta H_f(A^q, \varepsilon_F)$ is, the larger the equilibrium concentra- tion of $A^q$ . Positively-charged defects (donors) form more easily in p-type materials ( $\varepsilon_F$ near the VBM), but their for- mation releases electrons, thus contributing to n-type behavior. Nurstingly observed, defects (accentors) form	ment, and have greatly contributed to interaction with experiments. However, experimenting seems to lead the way by coming up first with practical dopants in GaN.
	behavior. Negatively-charged defects (acceptors) form more easily in n-type materials ( $\varepsilon_{\rm F}$ near the CBM [conduc- <u>tion_band minimum: 'shallow donor']), but their formation</u>	Semiconductors When two semiconductors AC and BC form an AC/BC
3	ly, the donor $(0/+)$ [or acceptor $(0/-)$ ] transition 'energy level' required to change the charge state. If the $(0/+)$ level is near the CBM, the system becomes n-type, whereas if	$\Delta E_v$ (AC/BC) = $E_v$ (AC)– $E_v$ (BC). The magnitude of the offset is an important device characteristic, as it determines the ability of electrons (in the conduction band) and
	'shallow acceptor'), the system becomes p-type. Deep donors or acceptors do not contribute carriers; fourthly, the migration barrier energy $\Delta H_m$ (A <sup>q</sup> , $\epsilon_F$ ) for diffusion of A <sup>q</sup> (the larger it is, the less mobile is A <sup>q</sup> ), and fifthly, the iden-	junction to the other. In the past few years, first-principles electronic structure theory has been applied to predict valence band and conduction band offsets between vari- ous materials either assuming an unstrained interface (leading to a featural band offset) or assuming schemet
<u></u>	Regarding 'n-type doping' via donors, theory found the following, firstly, $V_N^+$ (nitrogen vacancy) is a shallow donor, (producing upon ionization, electrons), but its formation energy $\Delta H_f$ ( $V_N^+$ ; n-type) is too high to warrant an appreciable carrier density, so $V_N^+$ is not the source of the observed n-type behavior. However, secondly, Si <sub>Ga</sub> and O <sub>N</sub> <sup>+</sup> (Si on Ga site; oxygen on N site) are much easier to	the calculations, and an-electron LAPW calculations pro- duce quite similar predictions, whereas the LMTO method sometimes gives somewhat different values. Let me first illustrate the situation, as well as the extent of agreement/disagreement with experiment by considering nitrides. LAPW calculations [28•] give for the 'natural' offset $\Delta E_v$ (InN/GaN) = 0.26 eV, whereas the pseudopo- tential values is 0.3 [29]. The LMTO value [30] is 0.51 eV.
	shallow donor states. Thus, these impurities are likely to be the reason for the observed n-type behavior. Thirdly, H <sup>+</sup> is a shallow donor, and its equilibrium lattice location	experimental values is generally excellent, often within 0.1 eV or so. This is the case for II-Vs [31] and most III-Vs [32]. Even in 'complicated' cases, where one calculates
	mation enthalpy permits a large equilibrium concentra- tion in p-type samples. The migration barrier $\Delta H_m$ is low (~0.7 eV), so H <sup>+</sup> is highly mobile. It compensates Mg <sub>Ga</sub> (see below).	ternary alloy (Ga <sub>x</sub> In <sub>1-x</sub> P) that can have different degrees $\eta$ of long range order, the agreement with experiment [34] is excellent. (In fact, the agreement with more recently mea- sured values is even better than with the older values. The calculated value did not change.)
	Regarding 'p-type doping' via acceptors, theory found the following, firstly, $V_{Ga}^{3-}$ (Ga vacancy) has a low formation energy, but its acceptor level is deep (~1 eV above VBM),	I would like to draw attention to three cases where the agreement between theory and the currently available
,	ered by attachment to $O_N$ (forming $v_{Ga}$ acceptor-donor pair). Secondly, H <sup>-</sup> has a shallow acceptor above the VBM, but its formation enthalpy in n-type material is high (lead- ing to limited solubility). It is almost immobile, due to a large $\Delta H_m$ . Hence, its ability to compensate donors such as Si <sub>Ga</sub> is limited. Thirdly, Mg <sub>Ga</sub> and Be <sub>Ga</sub> are shallow	Firstly, the measured $[35^{\circ}] \Delta E_v$ (GaN/InN) = 1.05 eV is con- siderably different from all first-principles values (0.26, [28 <sup>•</sup> ] 0.3, [29] 0.5 [30]). Secondly, the currently measured value for $\Delta E_v$ (InAs/GaAs) strained on an InAs substrate is - 0.57 eV [with $E_v$ (InAs) below $E_v$ (GaAs),] whereas LAPW
	enthalpies, and are thus predicted to lead to p-type	is $-0.04 E_v$ (InAs) being below $E_v$ (GaAs) whereas the LADW value is $+0.28 \text{ eV}$ [E. (LeAs) being above $E_v$ (CeAc)]

theory [32] produces a reverse order of band edges.

# Opinion

The three discrepancies between theory and experiment for Gan/Inin, GaAs/InAs and InSO/InSO are much target than the stated theoretical error bars, so the experimental determination (e.g. the degree of interfacial coherence maintained in the sample, and the accuracy of determination of the valence band edge) needs to be re-examined.

#### Spectroscopy of quantum dots explained

Semiconductor 'quantum dots' with typical dimensions of 20–100 Å can be synthesized as free-standing objects, or as semiconductor-embedded objects. Free-standing dots (e.g. InP, CdSe) are grown by colloidal methods, are strain-free, nearly spherical and have chemically passivated sur-

are grown by molecular beam enitaxy, are highly (but Progress made in the growth of 'free-standing' quantum

date and in the growth of comiconductor ambadded ('selfassembled') dots has opened the door to new and exciting spectroscopic studies of quantum structures. These have

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Coulomb blockade transitions. These new observations have created the need for developing appropriate theoretical tools capable of analyzing the electronic structure of  $10^3-10^6$  atom objects. The main challenge is to understand firstly, the way the one electron levels of the dot

and surface effects, and secondly, the nature of many particle interactions such as electron-hole exchange (underlying the 'red shift'), electron-hole Coulomb effects (underlying excitonic transitions), and electron-electron Coulomb effects (underlying Coulomb blockade effects).

In response to the challenges posed by these developments, a few theoretical models of the electronic structure of quantum dots were recently advanced. They are all based on the k·p method (see [37]), in which the wavefunction of the dot is expanded in Rerms of N<sub> $\Gamma$ </sub> bands of

(1-point). The method range from the effective mass

Norms and Dawendi [56] and Norms, *et al.* [59] and to  $N_{\Gamma} = 8$  of Jiang and Singh [40].

Most impressively, in their application to free-standing CdSe dots, Norris and Bawendi [38\*\*], succeeded in explaining, via the  $6 \times 6$  k·p method, the origin of as many as eight observed excitonic transitions in various size dots, and Jiang and Singh [40], and Grundmann, Stier and

Bimberg [41•] have explained the origin of the two main

In addition to explaining such 'one-electron properties,' an extended theory was recently able to explain the Stocks shift between absorption and emission as being due to electron-note exchange interactions [+2] (excitation can create either antiparallel, or parallel spins of the excited electron and the particle left behind. The splitting between these 'singlet' and 'triplet' configuration is due to exchange interactions, and is found to be dramatically enhanced in dots relative to bulk solids). An impressive success of theory in this regard is the identification of enhanced exchange interaction (as opposed to surface trapping) as the origin of the observed red shift.

In general, however, the exchange interaction contains a

with the e-h separation  $S = Jr_{e} - r_{e}J$ , and a long-range (LR)

wisdom [42\*\*] suggests that the LR exchange interaction in queptum dots originates as in bulk somiconductorfrom dipole-dipole coupling of the transition density between unit cells. Under this assumption, the LR contri-

fits well the observed red shift in CdSe nanocrystals. However, in the case of spherical zinc-blend quantum dots, the predicted  $1/R^3$  scaling of the red shift with size is not observed in either InP [43] or InAs nanocrystals. In both observed the observed scaling is  $R^{-2}$ 

# Opinion

The currently used 'theoretical technology' for understanding the electronic structure of quantum dots is based on the traditional k-p envelope-function approach with a limited basis of  $N_{\Gamma} < 8$  bands. Despite spectacular successes, it is unlikely that the details of the electronic structure of quantum-dot systems which lack periodicity in all three dimensions and exhibit surface effects as well as interfacial strain would be adequately described using a small number of 3D-periodic  $\Gamma$ -like bulk orbitals. This approach will ulti-

needed at the surfaces of the dots, non-1-like dot states

quantum confinement for sufficiently large dots will continue to be described very well by such approaches.

# Conclusions

Electronic structure theory of real materials has reached maturity, in that it is no longer preoccupied exclusively ----

	with methodological issues, but is actively engaged in explaining a wide range of materials properties, predict- ing unsuspected structures, and even challenging exper- imental data for correctness of assignment or interpreta-	<ol> <li>Car R, Parrinelio M: Unified approach for molecular dynamics and density-funtctional theory. <i>Phys Rev Lett</i> 1985, 55:2471-2474.</li> <li>Zungor A, Freeman AJ: Ground and excited state properties of LiF in the local density model. <i>Phys Rev B</i> 1977, 16:2901-2926.</li> <li>Neugebauer J, Van de Walle CG: Atomic geometry and electronic</li> </ol>
<u>, 1</u>	tations), the current attitude promises to signal the beginning of a new friendship' between experiment and	<ul> <li>23. Neugebauer J, Van de Walle CG: Role of hydrogen in doping GaN.</li> <li>Appl Phys Lett 1996, 68:1829-1831.</li> </ul>
•	theory.	In GalN (small migration enthalpy, i.e. highly mobile, shallow donor, located
	Papers of particular interest, published within the annual period of review, have been binblighted as:	focated near Ga antiponding site). It explains that $\text{Ivig}_{Ga}$ is compensated and passivated by H+.
	<ul> <li>of special interest</li> <li>of outstanding interest</li> </ul>	<ol> <li>Boguslawski P, Briggs EL, Bernholc J: Amphoteric properties of substitutional carbon impurity in GaN and AIN. Appl Phys Lett 1996, 69:233-235.</li> </ol>
	<ol> <li>Kohn W, Sham LJ: Self-consistent equations including exchange and correlation effects. <i>Phys Rev A</i> 1965, 140:1133-1138.</li> </ol>	<ol> <li>Boguslawski P, Briggs EL, Bernholc J: Native defects in GaN. Phys Rev B 1995, 51:17255-17258.</li> </ol>
	2. Ihm J, Zunger A, Cohen ML: A momentun: space formalism for the	26. Bernardini F. Fiorentini V. Bosin A: Theoretical evidence for efficient
	<ol> <li>Baroni S, Gianozzi P, Testa A: Green's function approach to linear response in solids. <i>Phys Rev Lett</i> 1987, 58:1861.</li> </ol>	The paper introduces the basic physics of Ga-substituted Be acceptors in GaN: it is a shallow acceptor (a good thing for p-doping), but $Be_3N_2$ is a
	<ol> <li>Singwi KS, Sjolander A, Tosi PM, Land RJ: Electron correlations at metallic clusters. IV. Phys Rev B 1970, 1:1044-1053.</li> </ol>	suggested that introduction of hydrogen would assist solubility. ?7. Mattila T. Nieminen RM: Point defect complexes and broad band
	<ol> <li>Hedin L, Lundqvist BI: Explicit local exchange-correlation potentials. J Phys C 1971, 4:2064-2083.</li> </ol>	28. Wei SH, Zunger A: Valence band splittings and band offsets of
	<ol> <li>Ceperley DM, Alder BJ: Ground state of the electron gas by a stochastic method. Phys Rev Lett 1980, 45:566-569.</li> </ol>	<ul> <li>AIN, GaN and InN. Appl Phys Lett 1996, 69:2719-2721.</li> <li>This is the basic paper on values, trends and underlying physics of the band offsets of AIN-GaN-InN in both zinc blende and wurtzite structures.</li> </ul>
	<ol> <li>Perdew JP, Zunger A: Self-interaction correction to density functional approximations for many-electron systems. <i>Phys Rev B</i> 1981, 23:5048-5079.</li> </ol>	<ol> <li>Van de Walle CG, Neugebauer J: Small valence band offsets at GaN/InGaN heterojunction. Appl Phys Lett 1997, 70:2577-2579.</li> </ol>
	<ol> <li>Phillips JC, Kleinman L: New method for calculating wave functions in crystals and molecules. <i>Phys Rev</i> 1959, 116:287-294.</li> </ol>	<ol> <li>Albanesi EA, Lambrecht WRL, Segall B: Theoretical study of the band offsets at GaN/AIN interfaces. J Vac Sci Technol 1994, 12:2470-2474.</li> </ol>
	<ol> <li>Topiol A, Zunger A, Rutner M: Local density pseudopotentials for first-raw atoms. Chem Phys Lett 1997, 49:367-373.</li> </ol>	<ol> <li>Wei SH, Zunger A: Chemical trends in band offsets of Zn and Mn based II-VI superlattices. <i>Phys Rev B</i> 1995, 53:R10457-R10460.</li> </ol>
	<del></del>	<ol> <li>Wei SH, Zunger A: InAsSb/InAs: a type I or a type II band alignment. Phys Rev B 1995, 52:2039-2044.</li> </ol>
	11. Hamann DR, Schluter M, Chiang C: Norm-conserving	33. Froven S. Zunder A. Mascarenhas A: Polarization fields and hand
<i>t</i> '	form factors for fourteen semiconductors of the diamond and	34. <u>Q'Shea JJ. Reaves CM. DenBaars SP. Chin Ma. Naravanamurti V:</u>
	<ol> <li>Wei SH, Krakawer H: Local-density-functional calculation of the pressure-induced metallization of BaSe and BaTe. <i>Phys Rev Lett</i> 1985, 55:1200-1203.</li> </ol>	spectroscopy. Appl Phys Lett 1996, 69:3022-3024.
*	14. Andersen OK: Linear methods in band theory. Phys Rev B 1975.	discontinuities of wurtzite GaN/AIN and InN heterojunctions
	<ol> <li>Methfessel M: Elastic constants and phonon frequencies of Si calculated by a fast full-potential linear-muffin-tin-orbital method.</li> </ol>	This paper created much controversy in the field, because its measured $\ln/GaN$ offset of $1.05\pm-0.25$ eV is 2 to 3 times larger than 'all' calculated
	16. Davidson ER: The iterative calculation of a few of the lowest	paper to infer the offset, is sufficiently accurate. The issue is still open.
	eigenvalues and corresponding eigenvectors of large real- symmetric matrices. J Comput Phys 1975, 17:87-94.	30. Onler C, Konleick K, Forster A, Luth H: Strain dependence of the valence band onset in Imas/GaAs neterojulctions teterimined by UV photoelectron spectroscopy. <i>Phys Rev B</i> 1994, <b>50</b> :7833-3837.
	17. Wood DM, Zunger A: <b>A new method for diagonalizing large</b> matrices. J Filys A 1965, 18.1343-1359.	97. Bastard C, Brum JA, Forroira R: In <i>Solid State Physics</i> . Edited by Turnbull D, Ehrenreich H. New York: Academic Press; 1991, <b>44</b> :224.
	18. Payne MC, Teter MP, Allan DC, Arias TA, Joannopolus JD: <b>Iterative</b>	e dependent ontical spectrum in CdSe quantum dots. Phys. Rev. R
	<ul> <li>molecular dynamics and conjugate gradients. <i>Rev Mod Phys</i> 1992, 64:1045.</li> <li>19. Bendt P, Zunger A: Simultaneous relaxation of nuclear geometries and electronic charge densities in electronic structure theories. <i>Phys Rev Lett</i> 1983, 50:1684-1688.</li> </ul>	<ul> <li>This paper uses the 6 × 6k,p method adapted from Efros and predicts the energies of as many as eight (!) excitonic transitions in CdSe dots as a function of size. The agreement with experiment, for the lowest excitons is spectacular.</li> </ul>

j.	<ul> <li>39. Norris DJ, Efros AL, Rosen M, Bawendi MG: Size dependence of</li> <li>exciton fine structure in CdSe quantum dots. Phys Rev B 1996</li> </ul>	42. Efros S, Rosen M, Kuno M, Nirmal M, Norris DJ, Bawendi M: Band- edge exciton in quantum dots of semiconductions with a
		72 ' Mar Fa
	40. Jiang H, Singh J: Strain distribution and electronic spectra of	account of the effects of short range exchange, shape and size of dot on the fine structure of the spectrum.
	<i>B</i> 1997, <b>56</b> :4696-4701.	43. Nirmal M, Norris DJ, Bawendi MG, Etros A, Rosen M: Observation of
i	dots: strain distribution, optical phonons, and electronic structure.	44 Nirmal M. Norris D.L. Rowandi MG. Efras A. Rosan M: Rand-adce
	contined state in an InAs pyramidal quantum dot, embedded in GaAs. It formed the basis for extensive comparisons with experiments being the first realistic description of the electronic structure of such dots. However, the	<ul> <li>54:4843-4856.</li> <li>45. Micic OI, Cheong HM, Fu H, Zunger A, Spragne JR, Mascarenhas A,</li> </ul>

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