Theoretical predictions of electronic materials and their properties

Alex Zunger

In this article, I first define the basic structure of modern 'firstprinciples theory of real materials' (including old references), and then I review recent applications to electronic materials. I argue that electronic structure theory of real materiale ha advanced to the point where bold predictions of yet unmade materials and of unsuspected physical properties are being made, fostering a new type of interaction with experimentalists. I review the basic characteristics of this new style of theory, illustrating a few recent applications, and express opinions as to future challenges.

Addresses

National Renewable Energy Laboratory, Golden, Colorado 80401, USA; e-mail: alex_zunger@nrel.gov

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Abbreviations

Introduction The scope and structure of first-principles theory of 'real materials'

aims at understanding material properties and processes from an atomistic quantum-mechanical point of view, retaining the complexity and specificity of actual solids, without loosing track of the underlying global trends and basic physics.

First-principles electronic structure theory of'real materials'

What's done?

The basic structure of electronic structure theory is drawn from text-book quantum-mechanics. A 'system' (atom, molecule, solid, nanostructure) is defined via its 'external ρ (a) which includes information on

comprising the system, plus, when appropriate, external (e.g. electric, magnetic) fields. One then sets up an effective single-particle Schroedinger equation:

numbers (Z and Z and Z and Z and Z and Z . N) of all Δ atoms Δ

where $V_{\text{screening}}$ is the systems response to V_{ext} . The screening potential, depends on the density matrix ρ . Where $\{\psi_i\}, \{\varepsilon_i\}$ are the single-particle wavefunctions and enerrespectively. Assuming at first (hence, a given $V_{ext}(\mathbf{r})$) and using a specific microscopic model of screening (c.g. the local density approximation [LDA] [1]), one solves Equation 1 iteratively, using the boundary conditions appropriate to the system at hand (e.g. periodic bulk solids, isolated quantum dots, etc.). Iterations are needed because $V_{sorening}$ depends on ρ and the latter is obtained from the wavefunctions ψ via ρ (r,r') = $\sum \psi_i^*(r)\psi_i(r')$. The sequence is; one assumes ρ , then computes $V_{\text{screasing}}(\rho)$, then solves Equation 1 to find $\{\psi_i\},$ then recomputes a new ρ from the latter, and continues to self-consistency. \Vhen self-consistency is attaincd for

obtains the total electron $+$ nuclear energy [2] of that geometry:

$$
E_{\text{tot}}\left\{R_{\alpha}, \alpha = 1...N\right\} = \sum_{i} \epsilon_{i} - \frac{1}{2}E_{H} - \frac{1}{4}E_{XC} + \frac{1}{2}E_{i-i} \quad (2)
$$

where the first term is the sum of single particle energies, E_H is the electron-electron Coulomb (Hartice) energy, E_{XC} is the exchange-correlation energy, and E_{i-i} is the ion-ion-energy. The forees on all N atoms are then obtained from E_{tot} ; one seeks the geometry that produces no forces:

$$
F_{\alpha} = \partial E_{\text{tot}} / \partial R_{\alpha} = 0 \tag{3}
$$

What's the input and what's the output?

Given the inputs, the N atomic number $\{Z_{\alpha}\}\$ and initial

the 'system' equilibrium geometry (R_{α}) , its eigenvalue spectrum $\{\varepsilon_i\}$, and total energy. Second derivatives of the total energy with respect to unit cell deformations yield elastic constants $\{C_{ii}\}\$, whereas second derivatives with respect to collective atomic displacements yield force constants, hence the phonon spectrum. Bonding information is gleaned from the charge-density.

$$
\rho(\mathbf{r}) = \sum_i \psi_i^*(\mathbf{r}) \psi_j(\mathbf{r})
$$

HIND IN THE PERIODE STREET, OF THE HINE TESPONDE methods [3]. This yields quantities such as pressure equation of states, strain deformation potentials, and polarizabilities. When the eigenvalues $\{\varepsilon_i\}$ are interpreted

 $i + V_{ext}(\mathbf{r}) + V_{screening}(\mathbf{r}, \rho) \Psi(\mathbf{r}) = \mathbf{E} \Psi(\mathbf{r})$

the systems energy level structure, the transition matrix

elements between levels i and j (hence, the optical

What made it possible?

spectrum).

structure of matter.

from conceptual to computational breakthroughs, as well as from progress in computer technology. The main enabling steps are as follows:

The advances the this case component of 'first-principles' electronic structure theory of real materials' possible range

1. The formulation of $V_{\text{screening}}$ in terms of the density ρ by Kohn and Sham [l].

2. The evaluation of the functional form of useful approximation to $V_{\text{screening}}$ { ρ }, for example, the early exchange and correlation functional of Singwi *etal* **[4]** and of Hedin and Lundqvist [S], and the most accurate one by Ceperley and Alder [6], and Perdew and Zunger [7].

3. The simplification of V_{ext} in terms of atomic pseudopotentials [8] that are calculable from well-defined (e.g. LDA) atomic models, [9-11] rather than empirically [12].

4. The formulation of nondivergent methods for evaluating E_{tot} and F_{α} of infinite systems (e.g. in momentumspace) [Z].

5. The development of efficient computational strategies to solve Equation 1, once general forms of V_{ext} and $V_{screening}$ are formulated. This includes plane-wave methods (e.g. $\lbrack 2 \rbrack$), LAPW (linear augmented plane wave) [13] and LMTO (linear muffin tin orbital) $[14,15]$.

6. The development of linear-algebra approaches to huge matrix problems underlying Equation 1, for example, iter- band structure.

> 7. The development of strategies for displacing atoms (Equation 3) simultaneously with refining charge densities

> the latter [19] with molecular dynamics by Car and Parrinello [20].

parallel architectures.

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The characteristics of current first-principles annroaches to prediction of materials

the classic solid state text books in a number of important ways.

the calculation, or to suspect that one is ting the right answer for the wrong reason,' because there are now a number of independent approaches that systematically give the same answers. These are the LAPW and converged pseudopotential calculations (unfortunately, there are still quite a few LDA-based methods around that are poorly implemented producing unreliable results.)

Realism is key

Text-book simplifications including one-dimensional models; spherical-potentials; nearly free-electron models; simple tight-binding and other 'elegant' and 'back of the envelope' constructs have given way to an approach that tackles the real complexity and diversity of matter, without loosing sight of the underlying physics.

The approach is reflective

Discrepancies with experiments are analyzed by searching for specific inappropriate physical inputs/assumptions, rather than by using empirical adjustments to cover-up our cic imparance For example when a turnped b was calculated early on [41] for Life (9.8 ev, instead of the measured and previously calculated 14.2 eV) using a 'right' method (LDA with no adjustments [21]), the analysis of this shocking discrepancy led to a deeper understanding of fundamental (self-interaction) corrections [21] to the underking formation. Similar disorat

The attitude is bold and interactive

This type of theory sometimes predicts unsuspected stable structures, or materials with previously unknown prop-

between the theoretical prediction and its experimental testing is often shorter than the duration of a PhD thesis.

described above characterize mostly the electronic structure theory of 'electronic materials,' that is semiconductors. Indeed, the structure-function relationships underlying

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Theory predicts defect properties in III-V nitrides

gral evaluation approximations), but focuses instead on

Nieminen [27] have used the pseudopotential LDA

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Thirdly, indirect experimental evidence discussed in [32]

theory [32] produces a reverse order of band edges.

Opinion

The three discrepancies between theory and experiment for Gafy/min, Gaas/mas and mob/mob are much large than the stated theoretical error bars, so the experimental determination (e.g. the degree of interfacial coherence maintained in the sample, and the accuracy of determination of the valence band edge) needs to be re-examined.

Spectroscopy of quantum dots explained

Semiconductor 'quantum dots' with typical dimensions of $20-100$ Å can be synthesized as free-standing objects, or as semiconductor-embedded objects. Free-standing dots (e.g. InP, CdSe) are grown by colloidal methods, are strainfree, nearly spherical and have chemically passivated sur-

are grown by molecular beam epitaxy, are highly (but

Progress made in the growth of 'free-standing' quantum مطع من اهروسيو هاع <u>of esmigonduator smbs</u> assembled') dots has opened the door to new and exciting spectroscopic studies of quantum structures. These have

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exenange-spinting, stram-muuteu spinting, anu Coulomb blockade transitions. These new observations have created the need for developing appropriate theoretical tools capable of analyzing the electronic structure of $10³-10⁶$ atom objects. The main challenge is to underad firetly the way the one electron levels

and surface effects, and secondly, the nature of many particle interactions such as electron-hole exchange (underlying the 'red shift'), electron-hole Coulomb effects (underlying excitonic transitions), and electron-electron Coulomb effects (underlying Coulomb blockade effects).

In response to the challenges posed by these developments, a few theoretical models of the electronic structure of quantum dots were recently advanced. They are all based on the $k \cdot p$ method (see [37]), in which the wavefunction of the dot is expanded in terms of N_{Γ} bands of

<u>**U**</u>-point. The method range from the effective mass

toniis anu dawenui [əo] anu tvoniis, *et ut.* [əə] anu N_{Γ} = 8 of Jiang and Singh [40].

Most impressively, in their application to free-standing CdSe dots, Norris and Bawendi [38**], succeeded in explaining, via the 6×6 k p method, the origin of as many as eight observed excitonic transitions in various size dots, and Jiang and Singh [40], and Grundmann, Stier and

Bimberg [41[°]] have explained the origin of the two main

In addition to explaining such 'one-electron properties,' an extended theory was recently able to explain the Stocks shift hetween absorption and emission as being due to electron-noie exenatige interactions [42] yexcitation can create either antiparallel, or parallel spins of the excited electron and the particle left behind. The splitting between these 'singlet' and 'triplet' configuration is due to exchange interactions, and is found to be dramatically enhanced in dots relative to bulk solids). An impressive success of theory in this regard is the identification of enhanced exchange interaction (as opposed to surface trapping) as the origin of the observed red shift.

In general, however, the exchange interaction contains a

with the e-h separation $S = |r_1 - r_2|$, and a long-range (LR)

wisdom [42**] suggests that the LR exchange interaction from dipole-dipole coupling of the transition density between unit cells. Under this assumption, the LR contri-

evenance

whereas the EK continuution is set to zero. This approach fits well the observed red shift in CdSe nanocrystals. However, in the case of spherical zinc-blend quantum dots, the predicted $1/R³$ scaling of the red shift with size is not observed in either InP [43] or InAs nanocrystals. In

Opinion

The currently used 'theoretical technology' for understanding the electronic structure of quantum dots is based on the traditional k-p envelope-function approach with a limited basis of $N_\Gamma < 8$ bands. Despite spectacular successes, it is unlikely that the details of the electronic structure of quantum-dot systems which lack periodicity in all three dimensions and exhibit surface effects as well as interfacial strain would be adequately described using a small number of 3D-periodic F-like bulk orbitals. This approach will ulti-

needed at the surfaces of the dots, non-1-like dot state

the exchange interaction. However, the global reatures of quantum confinement for sufficiently large dots will continue to be described very well by such approaches.

Conclusions

Electronic structure theory of real materials has reached maturity, in that it is no longer preoccupied exclusively

with methodological issues, but is actively engaged in explaining a wide range of materials properties, predicting unsuspected structures, and even challenging experimental data for correctness of assignment or interpreta-

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